# PEQ1

#### PURPOSE

Compute the real or complex component of the first derivative of the Weierstrass P elliptic function of a complex number (equianharmonic case with unit period parallelogram).

#### DESCRIPTION

The Weierstrass elliptic function is described in detail in the Handbook of Mathematical Functions (see REFERENCE section below).

#### SYNTAX 1

 $\text{LET} \langle ar \rangle = \text{PEQ1}(\langle xr \rangle, \langle xc \rangle)$ 

<SUBSET/EXCEPT/FOR qualification>

where <xr> is a number, parameter, or variable that specifies the the real component of the input;

<xc> is a number, parameter, or variable that specifies the the complex component of the input;

<ar> is a variable or a parameter (depending on what <xr> and <xc> are) where the computed values are stored;

and where the  $<\!\!SUBSET/\!EXCEPT/\!FOR$  qualification> is optional.

This syntax computes the real component.

## SYNTAX 2

LET <ac> = PEQI1(<xr>,<xc>)

<SUBSET/EXCEPT/FOR qualification>

where <xr> is a number, parameter, or variable that specifies the the real component of the input;

<xc> is a number, parameter, or variable that specifies the the complex component of the input;

<ac> is a variable or a parameter (depending on what <xr> and <xc> are) where the computed values are stored; and where the <SUBSET/EXCEPT/FOR qualification> is optional.

This syntax computes the complex component.

## EXAMPLES

LET AR = PEQ1(2,1) LET AC = PEQI1(2,1) LET AR = PEQ1(X,4) LET AC = PEQI1(X,4)

#### NOTE 1

The Weierstrass elliptic functions are computed using algorithm 549 from the ACM Transactions on Mathematical Software (see the REFERENCE section below).

#### NOTE 2

If the input value corresponds to a lattice point, an error message is printed and the output value is set to the largest real number on the machine.

#### DEFAULT

None

# SYNONYMS

None

#### RELATED COMMANDS

| PEQ    | = | Compute the real component of the Weierstrass elliptic function (equianharmonic case).  |
|--------|---|---|
| PLEM   | = | Compute the real component of the Weierstrass elliptic function (lemniscatic case).     |
| PLEM1  | = | Compute the real component of the first derivative of the Weierstrass elliptic function |
|        |   | (lemniscatic case).   |
| SN     | = | Compute the Jacobi elliptic function sn.  |
| RF     | = | Compute the Carlson elliptic integral of the first kind.                                |
| RD     | = | Compute the Carlson elliptic integral of the second kind.                               |
| RJ     | = | Compute the Carlson elliptic integral of the third kind.                                |
| ELLIP1 | = | Compute the Legendre elliptic integral of the first kind.                               |

# REFERENCE

"Algorithm 549: Weierstrass' Elliptic Functions," Eckhardt, ACM Transactions on Mathematical Software, vol. 6 (pp. 112-120).

"Handbook of Mathematical Functions, Applied Mathematics Series, Vol. 55," Abramowitz and Stegun, National Bureau of Standards, 1964 (chapter 18).

## **APPLICATIONS**

Special Functions

#### IMPLEMENTATION DATE

94/11

#### PROGRAM

X2LABEL DASH = COMPLEX COMPONENT TITLE WEIERSTRASS ELLIPTIC FUNCTIONS LINE SOLID DASH MULTIPLOT 2 2; MULTIPLOT CORNER COORDINATES 0 0 100 100 LET C = 0.5PLOT PEQ1(X,C) FOR X = 0.015 AND PLOT PEQ1I(X,C) FOR X = 0.015LET C = -0.5PLOT PEQ1(X,C) FOR X = 0.015 AND PLOT PEQ1I(X,C) FOR X = 0.015LET C = 10PLOT PEQ1(X,C) FOR X = 0.0015 AND PLOT PEQ1I(X,C) FOR X = 0.015LET C = -10PLOT PEQ1(X,C) FOR X = 0.0015 AND PLOT PEQ1I(X,C) FOR X = 0.0.015END OF MULTIPLOT

